## Math 431: Homework for Section 1.2

Due: Tuesday, August 26

## 1.\* If

$$\left[\begin{array}{cc} a+b & c+d \\ c-d & a-b \end{array}\right] = \left[\begin{array}{cc} 4 & 6 \\ 10 & 2 \end{array}\right],$$

find a, b, c and d.

 $2. \quad {\rm Let}$ 

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 1 & 4 \end{bmatrix}, \quad B = \begin{bmatrix} 1 & 0 \\ 2 & 1 \\ 3 & 2 \end{bmatrix}, \quad C = \begin{bmatrix} 3 & -1 & 3 \\ 4 & 1 & 5 \\ 2 & 1 & 3 \end{bmatrix}, \quad D = \begin{bmatrix} 3 & -2 \\ 2 & 4 \end{bmatrix},$$
$$E = \begin{bmatrix} 2 & -4 & 5 \\ 0 & 1 & 4 \\ 3 & 2 & 1 \end{bmatrix}, \quad F = \begin{bmatrix} -4 & 5 \\ 2 & 3 \end{bmatrix}, \quad O = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

If possible, computer the indicated operations:

- (a) C + E and E + C
- (b) A + B
- (c) D F
- (d) -3C + 5O
- (e) 2C 3E
- (f) 2B + F
- 3.\* Let O be the  $n \times n$  matrix all of whose entries are zero. Show that if k is a real number and A is an  $n \times n$  matrix such that kA = O, then k = 0 or A = O.
- 4. If A is an  $n \times n$  matrix, what are the entries on the main diagonal of  $A A^{T}$ ? Justify your answer.